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**BOOTSTRAP MISSPECIFICATION TESTS FOR ARCH  
BASED ON THE EMPIRICAL PROCESS OF SQUARED  
RESIDUALS**

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**Abstract**

We propose and study by means of simulations and graphical tools a class of goodness-of-fit tests for ARCH models. The tests are based on the empirical distribution function of squared residuals and smooth (parametric) bootstrap. We examine empirical size and power by means of a simulation study. While the tests have overall correct size, their power strongly depends on the type of alternative and is particularly high when the assumption of Gaussian innovations is violated. As an example, the tests are applied to returns on Foreign Exchange rates.

**Keywords:** ARCH models, empirical process, goodness-of-fit tests, size-power curves, smooth bootstrap, squared residuals.

*JEL Classification:* C12, C22.

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